

Generalizataion of Bertrand's conjecture

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Abstract

In 1845 Joseph Bertrand conjectured that for every integer $n > 1$ there is always atleast one prime p between n and $2n$ [1].

Mathematically there exists atleast one prime p such that $n < p < 2n$.

With the help of this conjecture we are going to generalize this

In this article we are going to show that for any prime p there exists atleast n primes between p and $2^n * p$.

Keywords: 1. Bertrand, 2. Conjecture, 3. Prime, 4. Generalization

INTRODUCTION

Bertrand had enunciated that there exists at least one prime between n and $2 * n$, more specifically there exists so between p and $2 * p$.

We are going to be more specific and showing the generalized version of Bertrand's Conjecture.

BODY OF THE WORK

There is at least a prime between p and $2 * p$.

So, there is also one between $2 * p$ and $4 * p$.

So between p and $4 * p$ there are atleast two .

More over between $4 * p$ and $8 * p$ there is another.

So between p and $8 * p$ there are atleast three.

Proceeding in this way we get there are atleast n so between p and $2^n * p$.

We are going to prove it in a more rigorous way , by the method of induction.

It is true for $n=1$, because there is atleast one between p and $2 * p$.

Let this be true for $n=m$.

So there are atleast m primes between p and $2^m * p$.

But according to Bertrand there is atleast one between $2^m * p$ and $2^{(m+1)} * p$.

So there are atleast $m+1$ primes between p and $2^{(m+1)} * p$.

So it is true for all n .

QED.

Conclusion

We conclude that there are atleast n primes between p and $2^n * p$.

Appendix

We conclude that there are atleast n primes between p and $2^n * p$.

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References

- [1] [https://www.cantorsparadise.com/bertrand's postulate](https://www.cantorsparadise.com/bertrand's%20postulate)
- [2] Elementary Number Theory , David M. Burton , Sixth edition , page no :-352.
- [3] heory of Numbers , Pundir and Pundir , page number 5.