

## **An Approach to Reduce the Variation in the Continuous Operating Voltages across Lightning Arrester Assemblies**

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### **Abstract**

Lightening arresters made of zinc oxide (ZnO) blocks are used to protect electrical equipments against lightening and switching surges. The continuous operating voltage (COV) is an important characteristic of the lightening arrester, which is the sum of the continuous operating voltages of the individual zinc oxide blocks used in the lightening arrester. An Indian electrical equipment manufacturing company was facing great difficulty in getting the correct combination of ZnO blocks for assembling lightening arresters. The major reason is the variation in COV between ZnO blocks. In this paper, the author discusses presents a solution to the aforementioned problem by providing a new approach for the selection of the ZnO blocks. The suggested approach significantly reduces the variation in COVs across arresters as well as the variation in number of ZnO blocks used across arresters. It also minimizes the usage of the total number of ZnO blocks under the given constraints and reduces the time taken to generate the required number of assemblies.

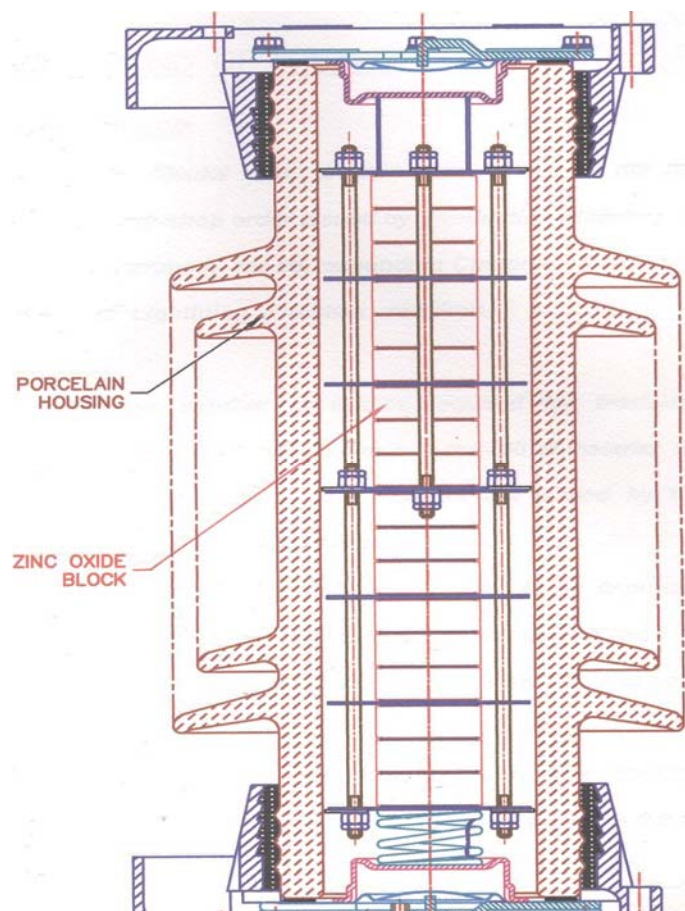
**Keywords:** Lightening Arrester, Zinc Oxide Blocks, Continuous Operating Voltage, Optimisation, Integer Linear Programming Problem, Lindo software

### **Introduction**

The electrical equipments often get damaged due to over-voltage. Lightening is one of the serious causes of over-voltage. If the power equipment, especially at outdoor substation is not protected, the over voltage will cause burning of insulations [1]. Lightening arrester is a device used to protect all electrical equipments and

installations, especially transformers, against lightning and switching surges in substations. The lightning arresters exhibit an extremely high resistance during normal operations and a very low resistance during transient over voltages [2]. Nowadays, the use of zinc oxide (ZnO) arresters, as a means of electrical equipment protection against over voltages due to lightning strikes, has been spread all over the world.

The ZnO lightning arrestors consist of zinc oxide blocks assembled in a porcelain housing and hermetically sealed. The section view of ZnO arresters is given in figure 1. ZnO blocks are highly purified, closely grained metal oxide powders, mixed; spray dried and then pressed to form discs & sintered at high temperatures. This process result in a dense polycrystalline discs. The basic molecular structure of the disc is a matrix of highly conductive zinc oxide and surrounded by highly resistive inter granular layer of other oxides. Under steady state conditions these barriers withstand the applied power frequency voltages, however under over voltage conditions they break instantly turning into conduction mode and divert surges to earth. The continuous operating voltage (COV) is an important characteristic of the lightning arrester, which is the sum of the continuous operating voltages of the individual zinc oxide blocks used in the lightning arrester.



**Figure 1:** Session of View Lightning Arrester

An Indian electrical equipment manufacturing company with a product range of insulators, bushings, transformers, wave traps, lightning arrestors, grading capacitors, surge capacitors, etc was facing great difficulty in getting the correct combination of ZnO blocks for assembling lightning arresters. The major reason was the variation in COV between ZnO blocks. The observed variation in COV was from 1.8 kilovolts (kV) to 2.8 kV across ZnO blocks. This, in turn, resulted in large variation in the number of blocks as well as in the COV between lightning arresters. For example, to full fill an order of 19 arresters with a COV of 303kV from the electricity supply and distribution board of a north-western state of India, the company used 130 to 145 ZnO blocks in different arresters and the COV varied from 303 kV to 307.8 kV between arresters as shown in table 1. Moreover the company used to spent two man-hours per day on segregation and selection of zinc oxide blocks for lightning arrester assembly, which amounts to Indian Rupees (Rs.) 72,000 annually. Hence this study was undertaken to minimize the variation in the COVs across lightning arrester assemblies as well as the variation in the number of ZnO blocks used across arresters.

**Table 1:** Lightning Arrester Assemblies generated using existing method

| Assembly Number | Number of ZnO blocks with different COVs used in the assembly |            |            |            |            |            |            |           |           | Total Blocks | COV    |
|-----------------|---|------------|------------|------------|------------|------------|------------|-----------|-----------|--------------|--------|
|                 | 2.4   | 2.35       | 2.3        | 2.25       | 2.2        | 2.15       | 2.1        | 2.05      | 2         |              |        |
| 1               | 0   | 2          | 0          | 0          | 0          | 51         | 77         | 14        | 0         | 144          | 304.75 |
| 2               | 0   | 0          | 0          | 0          | 0          | 0          | 125        | 10        | 10        | 145          | 303    |
| 3               | 0   | 0          | 5          | 1          | 61         | 67         | 7          | 0         | 0         | 141          | 306.7  |
| 4               | 0   | 0          | 76         | 52         | 1          | 0          | 0          | 5         | 0         | 134          | 304.25 |
| 5               | 0   | 45         | 80         | 2          | 1          | 0          | 0          | 2         | 3         | 133          | 306.55 |
| 6               | 1   | 0          | 44         | 84         | 5          | 1          | 0          | 1         | 0         | 136          | 307.8  |
| 7               | 0   | 3          | 0          | 0          | 0          | 95         | 41         | 2         | 2         | 143          | 305.5  |
| 8               | 0   | 0          | 0          | 88         | 40         | 7          | 1          | 1         | 0         | 137          | 305.2  |
| 9               | 1   | 3          | 89         | 38         | 3          | 0          | 0          | 0         | 0         | 134          | 306.25 |
| 10              | 0   | 0          | 6          | 124        | 6          | 0          | 0          | 0         | 0         | 136          | 306    |
| 11              | 0   | 0          | 0          | 80         | 47         | 6          | 2          | 0         | 2         | 137          | 304.5  |
| 12              | 0   | 0          | 0          | 0          | 0          | 72         | 60         | 11        | 0         | 143          | 303.35 |
| 13              | 0   | 0          | 49         | 81         | 4          | 0          | 0          | 1         | 0         | 135          | 305.8  |
| 14              | 0   | 0          | 0          | 71         | 56         | 8          | 0          | 1         | 1         | 137          | 304.2  |
| 15              | 0   | 1          | 0          | 81         | 51         | 4          | 0          | 0         | 0         | 137          | 305.4  |
| 16              | 1   | 0          | 48         | 81         | 4          | 0          | 0          | 0         | 1         | 135          | 305.85 |
| 17              | 0   | 49         | 81         | 1          | 0          | 0          | 1          | 0         | 0         | 132          | 305.8  |
| 18              | 0   | 93         | 36         | 1          | 0          | 1          | 0          | 0         | 0         | 131          | 305.75 |
| 19              | 8   | 122        | 0          | 0          | 0          | 0          | 0          | 0         | 0         | 130          | 305.9  |
| <b>Total</b>    | <b>11</b>   | <b>318</b> | <b>514</b> | <b>785</b> | <b>279</b> | <b>312</b> | <b>314</b> | <b>48</b> | <b>19</b> | <b>2600</b>  |        |

The remaining part of this paper is arranged as follows: the details of the existing assembly process and the suggested approach are given in section 2. The formulation of the problem is given in section 3. The validation of the suggested approach is presented in section 4 and the conclusion is given in 5.

## Approach

Through discussion with engineers, the step-by-step details of existing lightning arrester assembly process are identified as follows:

- Step 1 Draw ZnO blocks from store
- Step 2 Segregate and select blocks for assembly
- Step 3 Calculate the COV and count the number of blocks required
- Step 4 Check whether the number of blocks is less than or equal to the maximum specified number
  - If yes, proceed to next step
  - Else, go back to step 2
- Step 5 Check whether the COV is greater than or equal to required COV
  - If yes, proceed to next step
  - Else, go back to step 2
- Step 6 Check whether the ZnO blocks of different COVs is less than or equal to the number available
  - If yes, proceed to next step
  - Else, go back to step 1
- Step 7 Do stack assembly
- Step 8 Do Module Assembly
- Step 9 Leak and Electrical testing

It has been seen that there are 3 major loops (steps 4, 5 & 6) in the assembly process. The engineers pointed out that assembly process often enter into one or more of these loops and in many times lot of iterations are required to exit the loop, especially when the customer orders a batch of arresters with the same COV.

Based on the discussions and process details, the author felt that the selection of ZnO blocks for lightning arrester assembly is an optimization problem. Formulating and solving it as an optimization problem may yield a better result than the current practice of trial and error method for selecting ZnO blocks for assembly. A detailed literature survey [3 – 14] revealed that nobody has formulated the selection of ZnO blocks for lightning arrester assembly as an optimization problem. The company professionals are also unaware of any organization using optimization methods to arrive at the best combination of ZnO blocks for lightning arrester assembly. Hence it is decided to try this novel approach. The formulation of the problem is given in the next section.

**Problem Formulation**

The selection of ZnO blocks for assembling a batch of lightning arresters of a given COV is formulated as follows:

Let  $i = 1, 2, \dots, n$  be the number of lightning arresters to be assembled. Let the required minimum COV for every arrester be  $V$  and the variation in COV across arresters be  $V$  to  $V + \delta$ .

Let  $k$  be the maximum number of ZnO blocks allowed in a single assembly and the variation in the number of ZnO blocks between arresters be  $k - \nabla$  to  $k$ .

Let  $j = 1, 2, \dots, m$  be the different ZnO blocks with COVs of  $y_1, y_2, \dots, y_m$  and let  $A_j$  be the number of  $j^{th}$  ( $j = 1, 2, \dots, m$ ) ZnO block available in the store.

Let  $x_{ij}, i = 1, 2, \dots, n; j = 1, 2, \dots, m$  be the number of  $j$  (with COV  $y_j$ ) ZnO blocks used in  $i^{th}$  assembly.

Then the problem is to minimize the total number of blocks used for assembling the entire batch of arresters

$$\text{i.e. Minimize } z = \sum_{i=1}^n \sum_{j=1}^m x_{ij} \tag{1}$$

subject to the constraints

- 1 The number of ZnO blocks in each and every arrester should be between  $k - \Delta$  and  $k$

$$\text{i.e. } k - \nabla \leq \sum_{j=1}^m x_{ij} \leq k, \text{ for } i = 1, 2, \dots, n \tag{2}$$

- 2 The COV of each and every arrester should be between  $V$  and  $V + \delta$

$$\text{i.e. } V \leq \sum_{j=1}^m x_{ij} y_j \leq V + \delta, \text{ for } i = 1, 2, \dots, n \tag{3}$$

- 3 The number of times the  $j$ th ZnO block (with COV  $y_j, j = 1, 2, \dots, m$ ) used in assembling the entire batch of arresters should not exceed the number of the same available in the store

$$\text{i.e. } \sum_{i=1}^n x_{ij} \leq A_j, \text{ for } j = 1, 2, \dots, m \tag{4}$$

- 4 The number of ZnO blocks,  $x_{ij}, i = 1, 2, \dots, n; j = 1, 2, \dots, m$ , used should be integer and non negative

$$\text{i.e. } x_{ij} \geq 0, \text{ for } i = 1, 2, \dots, n; j = 1, 2, \dots, m \tag{5}$$

$$\text{i.e. } x_{ij} = \text{integer}, \text{ for } i = 1, 2, \dots, n; j = 1, 2, \dots, m \tag{6}$$

The aforementioned problem is an integer linear programming problem (ILP). ILPs [15-16] are linear programming programs with some or all variables are restricted to integer (discrete) values. This problem can be solved using any operations research packages like Lindo [17].

### Validation and Implementation

The new approach is tested with the same order of 19 arresters with a required COV of 303kV from the electricity supply and distribution board of a northwestern state of India. The result obtained is given in table 2. The comparison of table 1 & 2 revealed that the new approach used only 2579 blocks instead 2600 (reduction of 21 blocks). The variation in the number of blocks across the assemblies is also reduced (131 to 138 in new approach against 130 to 145 in old approach). Similarly the variation in COV across arresters also reduced (303kV to 304.65kV in new approach against 303kV to 307.8kV in old approach). Also the time taken to generate assemblies is also reduced to less than 5 minutes. Hence it is concluded that the new approach is superior to existing method of ZnO block selection for lightning arrester assembly.

The new approach is piloted with another order for 12 lightning arresters with a required COV of 268kV from the electricity supply and distribution board of a northern state of India. The assemblies generated using the new approach is given in table 3. It has been seen that the variation in the number of blocks across the arresters is only 5 (from 100 to 105) and the variation in COVs across the arresters is only 3.25kV (from 268kV to 271.25kV). Moreover the time taken to generate the assemblies is drastically reduced.

**Table 2:** Lightning Arrester Assemblies generated using new method

| Assembly Number | Number of ZnO blocks with different COVs used in the Assembly |      |     |      |     |      |     |      |    | Total Blocks | COV    |
|-----------------|---|------|-----|------|-----|------|-----|------|----|--------------|--------|
|                 | 2.4   | 2.35 | 2.3 | 2.25 | 2.2 | 2.15 | 2.1 | 2.05 | 2  |              |        |
| 1               | 0   | 58   | 52  | 21   | 0   | 0    | 0   | 0    | 0  | 131          | 303.15 |
| 2               | 0   | 27   | 70  | 35   | 0   | 0    | 0   | 0    | 0  | 132          | 303.2  |
| 3               | 0   | 22   | 69  | 36   | 0   | 3    | 3   | 0    | 0  | 133          | 304.15 |
| 4               | 0   | 0    | 77  | 37   | 2   | 9    | 9   | 0    | 0  | 134          | 303    |
| 5               | 2   | 0    | 75  | 37   | 1   | 10   | 9   | 0    | 0  | 134          | 303.15 |
| 6               | 0   | 37   | 9   | 41   | 15  | 16   | 17  | 0    | 0  | 135          | 303    |
| 7               | 0   | 34   | 10  | 41   | 15  | 18   | 18  | 0    | 0  | 136          | 304.65 |
| 8               | 0   | 28   | 10  | 43   | 19  | 18   | 18  | 0    | 0  | 136          | 303.85 |
| 9               | 0   | 9    | 11  | 44   | 22  | 23   | 23  | 5    | 1  | 138          | 303.85 |
| 10              | 0   | 14   | 13  | 45   | 20  | 21   | 21  | 3    | 0  | 137          | 303.45 |
| 11              | 0   | 14   | 13  | 45   | 20  | 21   | 21  | 3    | 0  | 137          | 303.45 |
| 12              | 0   | 14   | 13  | 45   | 20  | 21   | 21  | 3    | 0  | 137          | 303.45 |
| 13              | 0   | 14   | 13  | 45   | 20  | 20   | 21  | 3    | 1  | 137          | 303.3  |
| 14              | 0   | 14   | 13  | 45   | 20  | 21   | 21  | 3    | 0  | 137          | 303.45 |
| 15              | 3   | 11   | 13  | 45   | 20  | 21   | 21  | 3    | 0  | 137          | 303.6  |
| 16              | 0   | 14   | 13  | 45   | 20  | 21   | 21  | 3    | 0  | 137          | 303.45 |
| 17              | 3   | 11   | 13  | 45   | 20  | 21   | 21  | 3    | 0  | 137          | 303.6  |
| 18              | 0   | 14   | 13  | 45   | 20  | 21   | 21  | 3    | 0  | 137          | 303.45 |
| 19              | 0   | 14   | 13  | 45   | 20  | 21   | 21  | 3    | 0  | 137          | 303.45 |
| Total           | 8   | 349  | 513 | 785  | 274 | 306  | 307 | 35   | 2  | <b>2579</b>  |        |
| Available       | 12  | 356  | 517 | 797  | 284 | 317  | 314 | 51   | 20 | <b>2668</b>  |        |

**Table 3:** Pilot implementation result

| Assembly Number | Number of ZnO blocks with different COVs used in the Assembly |      |     |      |     |      |     |      | Total Blocks | COV    |
|-----------------|---|------|-----|------|-----|------|-----|------|--------------|--------|
|                 | 2.8   | 2.75 | 2.7 | 2.65 | 2.6 | 2.55 | 2.5 | 2.45 |              |        |
| 1               | 0   | 0    | 1   | 3    | 0   | 97   | 4   | 0    | 105          | 268    |
| 2               | 0   | 0    | 3   | 14   | 20  | 67   | 0   | 0    | 104          | 268.05 |
| 3               | 3   | 1    | 21  | 60   | 10  | 6    | 0   | 0    | 101          | 268.15 |
| 4               | 0   | 0    | 66  | 15   | 10  | 10   | 0   | 0    | 101          | 269.45 |
| 5               | 1   | 21   | 45  | 15   | 10  | 8    | 0   | 0    | 100          | 268.2  |
| 6               | 0   | 18   | 12  | 15   | 47  | 10   | 0   | 0    | 102          | 269.35 |
| 7               | 0   | 53   | 12  | 15   | 10  | 10   | 0   | 0    | 100          | 269.4  |
| 8               | 5   | 48   | 12  | 15   | 10  | 10   | 0   | 0    | 100          | 269.65 |
| 9               | 37  | 16   | 12  | 15   | 10  | 10   | 0   | 0    | 100          | 271.25 |
| 10              | 36  | 16   | 12  | 15   | 10  | 10   | 1   | 0    | 100          | 270.95 |
| 11              | 37  | 16   | 12  | 15   | 10  | 10   | 0   | 0    | 100          | 271.25 |
| 12              | 37  | 16   | 12  | 15   | 10  | 10   | 0   | 0    | 100          | 271.25 |
| Total           | 156   | 205  | 220 | 212  | 157 | 258  | 5   | 0    | <b>1213</b>  |        |
| Available       | 156   | 205  | 220 | 215  | 159 | 265  | 175 | 76   | <b>1471</b>  |        |

## Conclusion

In this paper, the author discusses a new approach for selecting the ZnO blocks for lightning arrester assembly. The suggested approach is to formulate and solve the problem as an optimization problem. The validation of the approach showed that there is significant reduction in the variation in COVs across arresters as well as the number of ZnO blocks used across arresters. Moreover the new approach minimizes the usage of the total number of ZnO blocks under the given constraints. The new approach also reduces the time taken to generate the required number of assemblies. This helped the organization to save two man-hours per day resulting in a monetary saving of Indian rupees 72,000/- annually.

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